Optimization of Hybrid Air-conditioning System with Natural Ventilation by GA and CFD

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ABSTRACT

This study aims at the development of an optimal design tool using a genetic algorithm (GA) and computational fluid dynamics (CFD). To represent a realistic building environment, random variables (fluctuating outdoor conditions), passive control variables (model variables) and active control variables (HVAC system) were set up. A combination of designs are determined based on the relationship between the fluctuating outdoor conditions and the HVAC system in the optimization inquiry. Building environment design should consider this relationship of active and passive control because the HVAC system works until the indoor climate reaches the target indoor climate when outdoor conditions are changing.

Keywords
Optimization, Genetic Algorithm (GA), Computational Fluid Dynamics (CFD)
Passive and active control elements, Random variables, Feed-back loop

1 Introduction

This study aims at the development of an optimal design tool using GA and CFD [2], [3], [4] for hybrid air-conditioning [1]. As elements to be considered in the design, there are the outdoor conditions, passive control elements for natural wind forced ventilation (such as the form of the inside and outside of the building), and active control elements of the indoor environment (such as HVAC system). Outdoor conditions are a fluctuating factor, and active control elements of the indoor climate (such as HVAC system) which are changing the output (boundary conditions of HVAC) in order to maintain the indoor climate at the target level for fluctuating outdoor conditions. This research treats the outside conditions as random variables, and examines the design variables selected by GA and actively changes the indoor situation corresponding to the outdoor conditions with a feed-back loop from the outputs of HVAC system control to the input boundary conditions of the CFD. This optimization method means that the feed-back loop of sensor and outputs of HVAC works until indoor climate is at the target level after GA has selected passive elements (design variables). The whole process of optimization consists of a two-step process to reduce the calculation load for finding the optimal solution. This study carried out a simple analysis using a coarse mesh considering the calculation load in the first step. In the second step, a detailed CFD analysis using a fine mesh was performed on the cases ranked top selected in the first step.

2 Optimization method Using GA and CFD

2.1 The optimization method
1. Setting up passive control elements for natural ventilation (design variables), active control elements (such as HVAC system), random variables (here mainly climatic conditions), restricting conditions and the objective function.
2. Design variables are selected by an optimization technique, and random variables are selected by a sampling technique.
3. CFD analysis is performed on the selected design variables and the selected random variables.
4. Active control elements are changed by the CFD feed-back loop, and the indoor climate is analyzed until it reaches the target value.
5. Restricting conditions and the objective function are evaluated.
6. Repeat loops 2-5 and the cases selected from the top rank which show a high value for the objective function in the first step.
7. In the second step, a detailed CFD analysis is performed on the selected cases.

3 Optimization Design Case Study

Assuming that the outdoor temperature is the changing factor, optimization is performed on a hybrid air-conditioning system [1] with natural ventilation in the mid-term.

3.1 Basic Model
The basic model for this study is shown in Figure 2 and Table 1. The width of the calculation area is set at half of the 3.6 m office module (1.8 m), considering of the symmetrical configuration. Hybrid air-conditioning is modeled as the outdoor air flows into the room from the upper opening of the window (0.5×1.8 m; Fig. 2, left), and is expelled through the opening at the other side (0.5×1.8 m; Fig. 2, right), while the HVAC is still operating. And the floor supply openings (0.1×0.2m) are set up. An I-shaped partition and a desk are installed. Personal computers and a human model are installed to represent the source of internal heat generation. In this study, The HVAC system in the room is assumed to be operating and the output of the HVAC is controlled by the CFD feed-back loop.
3.2 Design variables
Design variables for this study are shown in Figure 3. In this study, three design pattern elements are examined for the hybrid air-conditioning system with natural ventilation. These are the locations of the floor supply openings (6 patterns), the styles of the natural ventilation supply openings (5×5=25 patterns), there are two design variables which are width and height of the natural ventilation) and the styles of the window (5×(2×12-1)=115 patterns, there are three design variables which are the width and height of the window and the window start line which are 0.8 m and 2.0 m). The total number of design patterns is 17250.

3.3 Random variables
This study considers only the outdoor temperature which is based on the weather data of the Japan Meteorological Agency from May to June. The wind induced ventilation rate is assumed to be constant with the device of constant volume. The data for the random variables are selected by taking one hour intervals from 8:00 to 18:00. The moment design method was used for selecting random variables according to the average changes in the distribution and standard deviation of the outdoor conditions in this study, and on the assumption of instantaneous diffusion conditions without considering the influence of thermal storage in the building structure. The probability of a random variable is used as a weighting factor, which is multiplied by the objective function. The statistical value of the objective function is calculated with changing outdoor conditions taken into account. In this study, only the range ±2σ (95.4% of the entire ranges) is based on the mean value (M) of the outdoor temperature. The sampling interval and random variables are shown in Table 2.

![Figure 2: Basic model (Units:m)](image1)

![Figure 3: Design variables (Units:m)](image2)

<table>
<thead>
<tr>
<th>Table 1 Heat sources (Basic model)</th>
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<tr>
<td>Heat sources</td>
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<tr>
<td>Quantity of heat</td>
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- Floor area of 19.4 m² produces 88 W/m² of sensible heat
- Human model is a cube of dimensions 0.45m×0.33m×0.88m

<table>
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<tr>
<th>Table 2 Random variables</th>
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<tr>
<td>Sampling interval</td>
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<tr>
<td>-2σ → -σ</td>
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<tr>
<td>-σ → M</td>
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<tr>
<td>M → -σ</td>
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<tr>
<td>σ → -2σ</td>
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</table>

Mean value(M) = 22.43 °C, Distribution (σ) = 0.977 °C, Standard deviation (σ) = 0.99 °C
4 Setting the Optimal Design

4.1 Objective function
The single objective function is the amount of energy-input to the HVAC system. The objective function is as follows:

\[ E(kW) = C_p \times \rho \times \Delta T \times Q \]  (1)

- \( C_p \): Constant-pressure ratio heat of air \([J/kg \cdot K]\)
- \( \rho \): Density of air \([kg/m^3]\)
- \( \Delta T \): Difference in temperature on outflow and inflow temperature of HVAC system \([K]\)
- \( Q \): The amount of wind on inflow of HVAC system \([m^3/s]\)

The optimal evaluation is achieved when the amount of energy-input in equation (1) reaches a minimum.

4.2 Restricting conditions
The restricting conditions set for the indoor environmental design in this study are as follows:
- The target temperature is 26.0°C (±0.2°C) in the task region.
- The size of window is over than 2.8m² a seventh of floor area.
- The average wind velocity is below 0.5 m/s in the task region.
- The limit wind velocity is below 2.0m/s on floor supply opening.
- The vertical difference in temperature is below 3.0°C in the task region.

Here, the task region is \( X_1 = 0.9-10.8 \) m, \( X_2 = 0.0-1.5 \) m, and \( X_3 = 0.0-1.8 \) m. The number of air changes per hour for the natural ventilation is fixed at 10 times, and the floor supply openings are fixed at 19°C.

4.3 GA and CFD analysis conditions
A multi-island genetic algorithm [4] is used in the first step for optimization. The detailed setup is shown in Table 4 and the boundary conditions of the CFD are shown in Table 5. The flow field is analyzed with three-dimensional CFD based on a standard k-ε model.

<table>
<thead>
<tr>
<th>Table 4 Setting the multi– island GA</th>
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<tbody>
<tr>
<td>Size of Sub-Population</td>
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<tr>
<td>Number of Islands</td>
</tr>
<tr>
<td>Number of Generations</td>
</tr>
<tr>
<td>Rate of Crossover</td>
</tr>
<tr>
<td>Rate of Mutation</td>
</tr>
<tr>
<td>Rate of Migration</td>
</tr>
<tr>
<td>Interval of Migration</td>
</tr>
<tr>
<td>Total</td>
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<table>
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<tr>
<th>Table 5 Boundary conditions for the CFD simulation</th>
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</table>
| INLET \( K_{in} = 3/2 \times (U_{in} \times 0.05)^2, \ v_{in} = C_\mu^{3/4} \times K_{in}^{3/2} / l_{in} \)
| \( l_{in} \): One seventh of the opening width
| \( U_{in} \): Velocity of inflow \([m/s]\), \( C_\mu \)= 0.09 |
| OUTLET \( U_{out} \): Mass balanced, Tout, kout , \( e_{out} \): Free slip |
| Wall, human model \( \text{Generalized log-law (Wall Function), Free slip at symmetric plane. Heat flux of human body and floor is fixed.} \)
| Turbulence model \( \text{High reynolds number k-ε model} \)
| Difference scheme \( \text{First-order upwind difference} \)
| Mesh \( 1^{\text{st}} \): 55(X₁)×25(X₂)×16(X₃)= 22000
| \( 2^{\text{nd}} \): 78(X₁)×35(X₂)×22(X₃)= 72000 |

\( k \): kinetic energy of inflow \([m^2/s^2]\), \( \varepsilon \): kinetic energy dissipation rate \([m^2/s^3]\), \( \text{in: inlet out: outlet} , T: \) temperature \([K]\), \( U: \) velocity of inflow \([m/s]\), \( l: \) specific length scale \([m]\)
4.4 Feed-back loop

The HVAC system is set so that a sensor is in agreement with the target temperature until the indoor temperature reaches 24 °C (Heating) and 26 °C (Cooling) in the hybrid air-conditioning model room with the feed-back loop of CFD. It is set so that the AC supply temperature is 19 °C for cooling and 26 °C for heating. The amount of supply air is controlled.

4.4.1 The convergence evaluation standard of the feed-back loop

- **Cooling**: The mean temperature in the task region is 26 °C (The accuracy is less than ±0.2 °C).
- **Heating**: The mean temperature in the task region is 24 °C (The accuracy is less than ±0.2 °C).
- **None HVAC system**: The amount of HVAC supply air is 0 (Q<0.001m³/s). When the mean temperature is 24ºC-26ºC in the task region with the amount of supply air which is 0.001 m³/s.

4.4.2 The standard for changing the HVAC setting between cooling and heating in the feed-back loop

- **Changing from cooling to heating**: Even if the amount of supply air (Cooling) is set to 0 (Q< 0.001m³/s), when the mean temperature of a task region is less than 24°C.
- **Changing from heating to cooling**: Even if the amount of supply air (Heating) is set to 0 (Q < 0.001m³/s), when the mean temperature in the task region is more than 26 °C.

4.4.3 The detailed feed-back loop

\[
Q_{NEW} = Q_{OLD} + \Delta Q
\]

\[
\Delta Q = \frac{[(T_{TASK} - T_{TARGET}) \times V_{TASK}]}{[(T_{TASK} - T_{SUPPLY}) \times \tau(s)]}
\]

- **Q_{NEW}**: The modified amount of wind [m³/s].
- **Q_{OLD}**: The amount of wind before modifying [m³/s].
- **\Delta Q**: The up and down amount of wind [m³/s].
- **T_{TASK}**: The mean temperature of task region [ºC].
- **T_{TARGET}**: The target temperature of the HVAC system [ºC].
- **V_{TASK}**: The volume of task region [m³].
- **\tau**: The relaxation time [s].

5 Simulation Result

5.1 GA and CFD analysis conditions

The results of the optimal design in the first step by multi-island GA and CFD are shown in Figure 4. The top three cases are selected in the first step for a detailed CFD analysis using a fine mesh in the second step.

5.2 The design selected in the first and second step

The design selected in the first step is shown in Table 6. The simulation result shows that the objective function is low when a larger natural ventilation opening is selected. It is assumed that the amount of sensible heat removal increases when the natural ventilation opening becomes larger. The floor supply openings are selected according to the relationship between the natural ventilation opening and the window. When the natural ventilation opening becomes small, there is a tendency for the number of floor supply openings to increase. And the amount of energy-input increases when the outside temperature becomes
high. In this study, Case A where the purpose function is the highest in step 2 search serves as the optimal design. The CFD analysis results of Case A are shown from figures 5 to 8.

<table>
<thead>
<tr>
<th>Cases selected in the first step (Unit: kw)</th>
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<tbody>
<tr>
<td>1Step</td>
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<tr>
<td>-------</td>
</tr>
<tr>
<td>A</td>
</tr>
<tr>
<td>B</td>
</tr>
<tr>
<td>C</td>
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<td>D</td>
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6 Conclusions
A hybrid air-conditioning system with natural ventilation in the mid-term was investigated as an example of the optimal design.

The optimal inquiry based on fluctuating factor outdoor conditions as the random variables, the building form as the passive control, and an HVAC system as the active control was performed, and its validity was demonstrated.

A two-step inquiry using a genetic algorithm showed that it was possible to produce an optimal design with a reduction in the calculation time.

The energy-saving effect of the hybrid air-conditioning system using natural ventilation in the mid-term was clarified.

References