

Influence of Computational Parameters on the Evaluation of Wind Effects on the Building Envelope*

APPUPILLAI BASKARAN†
TED STATHOPOULOS‡

This paper systematically examines the influence of the computational parameters on the computed wind loads on the building envelope. Parameters considered include: size of the computational domain, number of computational grid nodes, criteria used for the convergence of an iterating process and computing time requirements for different computer systems. In all four cases, computed results and computational cost (CPU time) are analyzed and for some cases comparisons are also made with the experimental data. By using this analysis a diagnostic system to monitor the computed results can be developed.

NOMENCLATURE

a_p	hybrid difference scheme coefficient at node P
B	building width
C_p	mean pressure coefficient
H	building height
k	turbulence kinetic energy
l_R	recirculation length from leeward side of building
L	building length
n_p	number of nodes surrounding P
NX, NY, NZ	total nodes on x, y and z directions
p	fluid pressure
P	grid node under consideration
R_p	imbalance in the conservation of mass
R_ϕ	residual source
S_L	linearized source term
t	time
u, v, w	mean velocity components along x, y, z direction
u_g	velocity at gradient height
U_H	velocity at roof height
x, y, z	distance along the co-ordinate axis
z_g	height of the boundary layer

Greek symbols

$\delta x, \delta y, \delta z$	grid distances between nodes
ε	dissipation of turbulent kinetic energy
ϕ	dependent variable, i.e. u, v, w, k, ε

Abbreviations

USD	Up-Stream Distance
DSD	Down-Stream Distance
DT	Distance from the building Top
DS	Distance from the building Side
MIPS	Millions of Instructions per Second.

*The authors prepared the paper on behalf of the National Research Council of Canada, and therefore the copyright in the paper belongs to the Crown in right of Canada, i.e. to the Government of Canada.

†Institute for Research in Construction, National Research Council of Canada, Ottawa, Ont., Canada, K1A 0R6.

‡Centre for Building Studies, Concordia University, Montreal, P.Q., Canada, H3G 1M8.

1. INTRODUCTION

A SYSTEMATIC approach is necessary to understand the products of nature and their consequences in human life. Wind is not only an integral part of human survival, it also has significant effects when it flows around buildings. Three major wind-induced effects on buildings (structural, environmental and energy) are listed in Fig. 1. It is the responsibility of a building engineer to design a safe and economical building taking these effects into consideration. So engineers need information regarding these wind-induced effects on buildings during the design process. This information is available through wind loading standards and codes of practice, which are based on data from various systematic wind tunnel experiments, sometimes confirmed by full scale measurements.

Improvements in computer resources offer a new and feasible tool for the evaluation and understanding of wind effects on buildings. However, it was only recently that studies (Vasilic-Melling [1], Hanson *et al.* [2, 3], Summers *et al.* [4], Paterson and Apelt [5, 6], Murakami *et al.* [7, 8], Mathews and Meyer [9], Baetke [10], Baskaran and Stathopoulos [11] and Baskaran [12]) have been made to simulate wind flow conditions around buildings using computers. This lack of utilization of the booming computer resources by the wind engineering research society is probably due to not only the complexity of the problem but also the difficulties involved in numerical modelling of the turbulence process, as explained by Hunt [13].

Numerically simulated results depend on many factors. A diagnostic system is often necessary to monitor the computed results. Numerical modelling of wind flow conditions around buildings mainly consists of three stages of operation, as shown in Fig. 2. These are: formulation stage, computation stage and validation stage. Each stage involves various sub-stages, some of which are displayed in the figure. The diagnostic system should be capable of

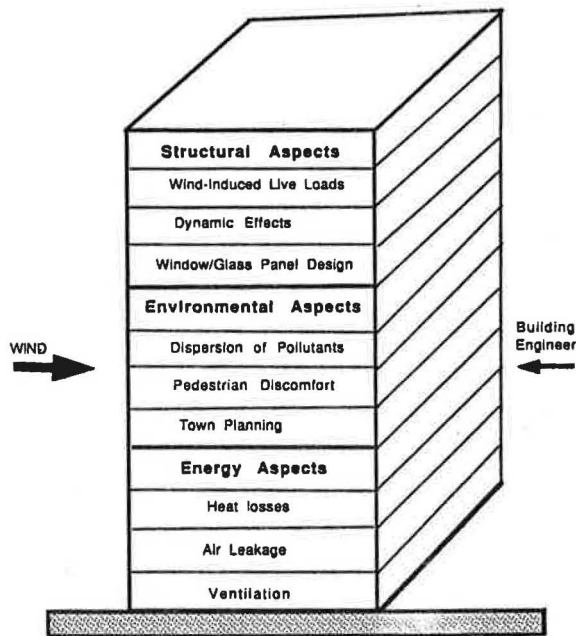


Fig. 1. Perspective of wind induced effects on buildings.

identifying and filtering the error introduced during each of these processes.

For the formulation stage, research efforts [14] have been made in the past to identify the influence of the various approximations of the Navier-Stokes equations. Raithby [15] critically evaluated different schemes used for the convective term interpolation and three schemes

were also applied and compared for the computation of steady state recirculating flows by Leschziner [16]. Turbulence modelling has also been well scrutinized by the computational group of Imperial College of Science and Technology in London [17, 18, 19]. For engineering applications, the well known $k-\epsilon$ models are found to be the ideal choice, considering the computational cost and the accuracy of the computed results. Authors who contributed to *Building and Environment* (Vol. 24, No. 1, 1989) Special Issue, "Numerical Solutions of Fluid Problems Related to Buildings, Structures and the Environment" were also in favour of $k-\epsilon$ turbulence model for the wind flow conditions around buildings.

Validation of the computed results is also an integral part of the numerical simulation. It can be performed by comparing the results with full scale measurements or, more often, by using data from wind tunnels. Summers and co-workers [4] performed a direct validation process for their simulated results. For comparison purposes, a simple wind tunnel model was fabricated and pressures and velocity were measured at the same locations as the computation [20]. Extensive comparisons in Ref. [4] clearly show the complexity involved in the validation stage, even for a simple building configuration. To exclude the modelling problems in the wind tunnel such as scale effects and turbulence intensity, Richards [21] compared the computed results using the data from a full scale "experimental station" on a low-rise building. His computed results were obtained by using Spalding's commercial code PHOENICS [22].

In this paper a systematic analysis has been made to identify the influence of computational parameters on the computed wind effects on buildings. Considered par-

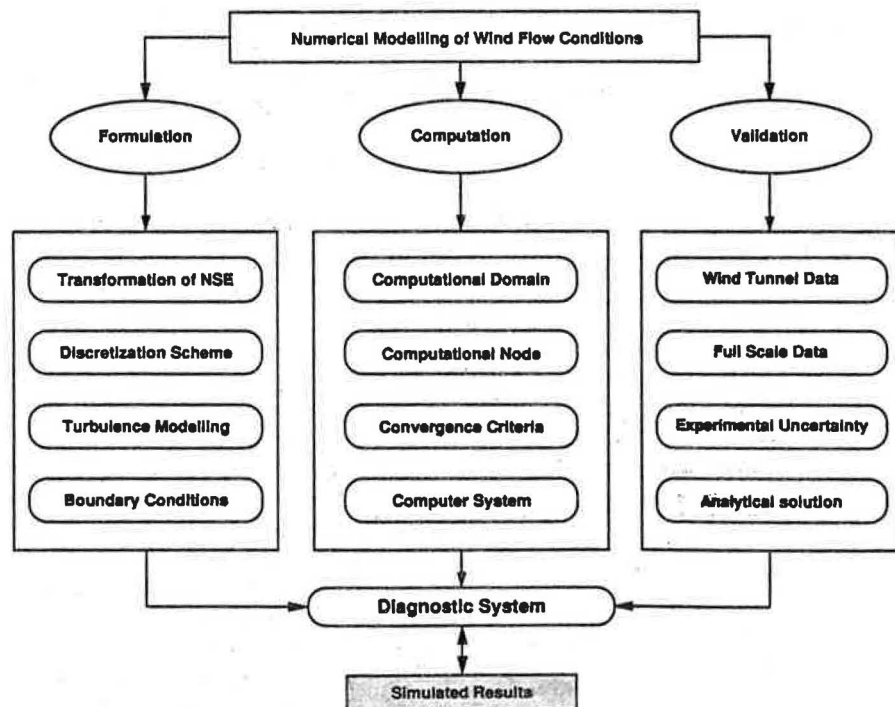


Fig. 2. Components of a diagnostic system for the numerical modelling of wind flow conditions around buildings.

ameters include the size of the computational domain, the number of computational grid nodes, the criteria used for the convergence of an iterating process and computing time requirements for different computer systems. In all four cases, both the computed results and the computational cost (CPU time) are analyzed; for some cases, comparisons are also made with the experimental data. Due to the complexity of the problem considered, observations are summarized based on the analysis of these parameters and no general guidelines are formulated. However, using these observations, one can develop a diagnostic system to monitor the computed results. The following section present a brief summary of the computational methodology, whereas the rest of the paper is dedicated to the analysis of the computational parameters.

2. COMPUTATIONAL METHODOLOGY

This section only outlines the computational procedure; more details can be found in Baskaran [12]. By using the control volume method of Patankar and Spalding [23], the differential equations are transformed into difference form. The final algebraic equation is written:

$$a_p \phi_p = \sum_{m=1}^{n_p} a_m \phi_m + S_L \quad (1)$$

in which P is the grid node where the dependent variable ϕ_p is computed, n_p is the number of nodes surrounding P , a_p is the hybrid difference scheme coefficient and S_L is the linearized source term.

The well known SIMPLE algorithm of Patankar [24] is used to correct the velocity field and also to improve the initially assumed pressure field. The advantageous staggered grid arrangement is used. For boundary conditions, the wall functions of Launder and Spalding [25] are used for the velocity variables and the newly developed zonal treatment method of Stathopoulos and Baskaran [26] is used for the turbulence variable to bridge the boundary nodes with the computational domain.

All computations were performed using the computer code TWIST—Turbulent WInd Simulation Technique—which consists of three modules respectively performing pre-processing, main computation and post-processing shown diagrammatically in Fig. 3. These three modules coded in ANSI Fortran-77 can run individually or in sequence. The post-processing module 3 frequently calls appropriate graphics subroutines during its operations. Modules 2 and 3 need more computer storage capacity in comparison with module 1, whereas module 2 takes the highest CPU time among the three. The main advantage of the modular structure is that the user can extend the code for any particular problem of interest, by adding new modules to an existing one.

A single building model about 14 cm high and 15 × 15 cm cross-section (56 × 60 × 60 m in full scale) is considered as the test case. Computations are performed for a power law inlet velocity profile having exponent 0.16, with a free stream wind speed of 12 m/s at a wind tunnel gradient height of 60 cm. Figure 4 shows a typical grid cluster for the considered test case, both in plan (xy) and

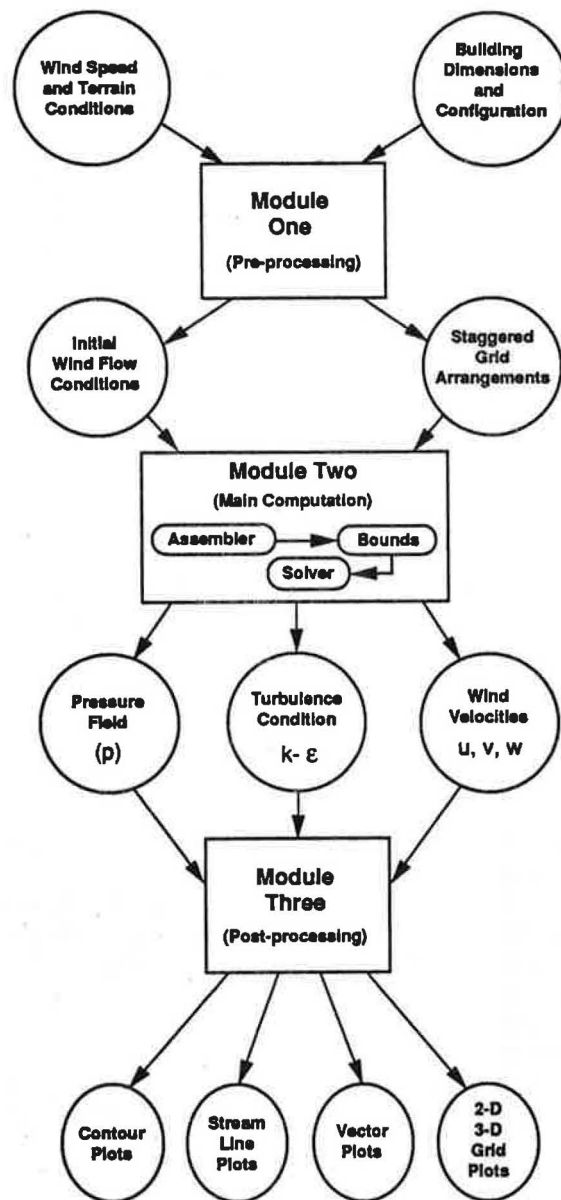


Fig. 3. The three modules of TWIST.

sectional (xz) views; the grid distances δx , δy and δz are not equal. Indeed, a non-uniform grid is often desirable. The misconception that non-uniform grids lead to less accuracy than uniform grids has no basis. In general, an accurate solution can be obtained only when the grid distribution is sufficiently fine. There is no need to use a fine grid in regions where the dependent variable changes rather slowly, such as the velocity above the gradient height. On the other hand, a fine grid is required near the windward wall or the roof of a building for numerical approximation of the high gradients. These basic ideas are taken fully into consideration during the grid generation, as can be clearly identified from the figure. Moreover, by using less grid spacing near the solid boundaries and arranging for non-uniform spacing in other regions, the efficiency of the computation is increased.

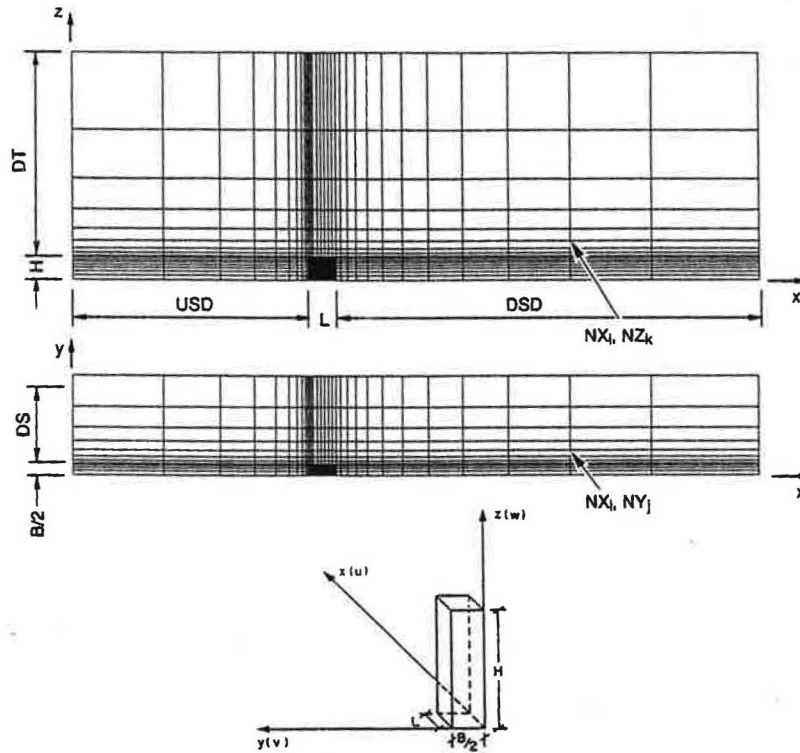


Fig. 4. Computational mesh distribution and co-ordinate system used.

The co-ordinate system used in the computational procedure is also indicated in Fig. 4. The x -axis carries the streamwise velocity; the lateral and vertical velocities follow the y and z directions, respectively. An Up-Stream Distance (USD) from the windward wall and a Down-Stream Distance (DSD) from the leeward wall define the boundaries of the computational domain along the x direction. For other directions, distances DS and DT are used as shown in the figure. Note that (NX_i, NY_j) is a node in the plan view (xy direction) which has $(NX \cdot NY)$ total nodes. Similar explanations also apply for sectional view.

3. EFFECT OF COMPUTING PARAMETERS

The effect of computing parameters is addressed by considering four main factors of the computation stage (see Fig. 2): size of the computational domain, number of computational nodes, criteria of terminating the iteration process and the use of different computer systems.

3.1. Influence of domain size on the computed results

The influence of the domain size is analyzed first, because experimental data are available which can be used as preliminary information for the numerical solution. Systematic studies (Hunt and Smith [27], Hunt [28]) were initiated during the early 70s for the understanding of wind generated wakes around a building and were continued by Lemberg [29], Penwarden and Wise [30] and Gandemer [31]. Beranek [32] grouped some of these results for the determination of the influence area for wind flow around tall slender buildings, tall buildings of transitional type, which have a significantly smaller

dimension along the flow direction than along the other two directions, and long buildings. These general guidelines are taken into account by the present study for the determination of the computational boundaries.

As listed in Table 1 four domain sets are considered in the analysis. The extent of the computational domain along the x , y and z directions is shown for each domain. During this exercise, other parameters namely the total number of nodes (81,600) and the convergence criterion (0.2) are kept constant. The DD2 set is selected based on the 2-D experimental study by Antoniou and Bergeles [33] and Bergeles and Athanassiadis [34] and it is consistent with the previous computational work of Paterson [5, 6] and Murakami *et al.* [7, 8]. With DD2 as the base, the effects on the computed results of increasing as well as decreasing the domain size were analyzed.

Figure 5 shows the streamline plots for the four cases considered. These plots show the side view pattern of flow distribution for a plane passing along the center of the building which is exposed to normal wind flow conditions. The plots are obtained using the converged

Table 1. Specifications of the different computational domains used in the present study

Set	x USD	x DSD	y DS	z DT
DD1	3 L	6 L	3 B	3 H
DD2	6 L	12 L	5 B	4 H
DD3	10 L	20 L	8 B	6 H
DD4	13 L	26 L	10 B	9 H

Number of nodes: 81,600
Convergence criterion: 0.2

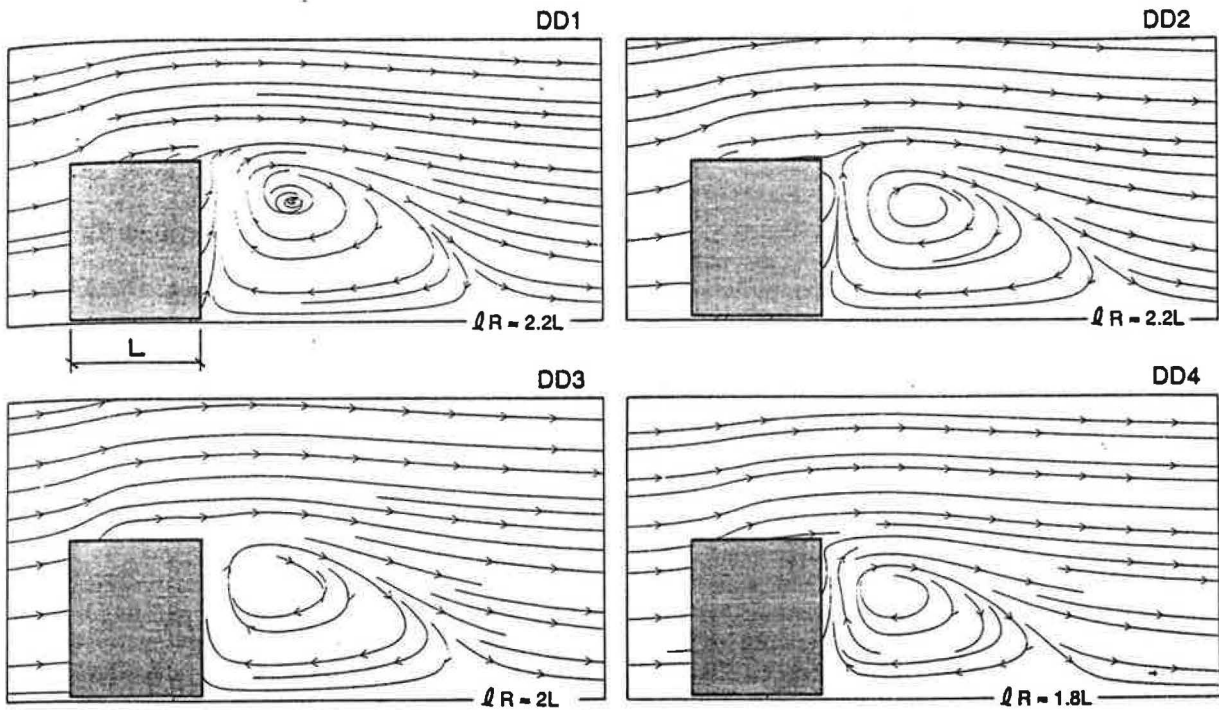


Fig. 5. Side view of streamline plots for different computational domains.

velocity components u and w . In all four figures the incoming flow separates from the leading edges and then forms recirculations behind the building. Overall, no significant differences are noted among the four figures. However, the recirculation zone of DD4 is smaller in comparison to the others. To quantify these changes, the length of recirculation is calculated as explained in Vasilic-Melling [1], by specifying the distance from the leeward wall, to the point where $u/u_g = 0.0$. These locations can also be easily identified from the streamline

plots; the respective recirculation lengths were equal to $2.2 L$, $2.2 L$, $2 L$ and $1.8 L$ for DD1, DD2, DD3 and DD4. Increasing the domain from DD2 decreases the length of recirculation. To support this description of the wake flow behavior, experimental evidence of flows over buildings, such as flow visualization techniques, will be necessary.

The induced pressure values were also analyzed for the variation in the domain distances, as shown in Fig. 6. The windward wall positive pressures, and suction induced

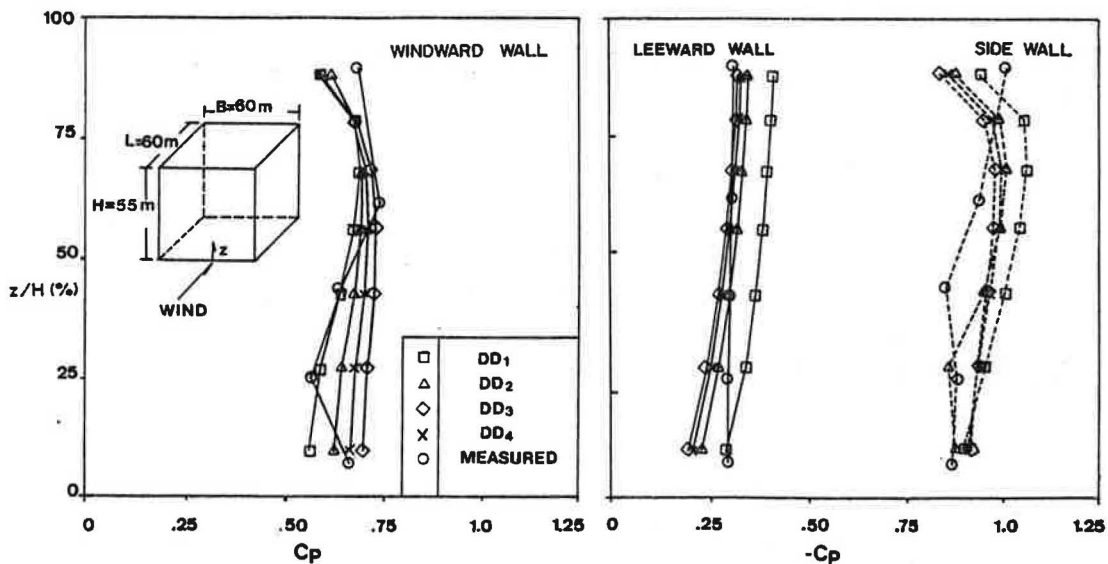


Fig. 6. Computed pressure coefficients on the building walls with different computational domains.

Table 2. Specifications of the different grid distributions used in the present study

Set	NX	NY	NZ	Total
NN1	38	20	28	21,280
NN2	48	22	32	33,792
NN3	58	26	36	54,288
NN4	68	30	40	81,600
NN5	78	36	40	112,320

Domain specification: DD2
Convergence criterion: 0.2

both on the leeward and side walls are shown in the figure. All the results are presented in the form of pressure coefficients, normalized by using the dynamic pressure at the building roof height. The maximum difference among the four sets was found for the pressure nodes near the ground level of the front wall. The DD1 curve is always away from the others, irrespective of the building wall and the pressure coefficient values are not significantly affected when the domain distances are increased beyond DD2. When comparing the observations of this figure, including the experimental results, selection of DD2 domain for further examination of the problem appears to be a good choice. In addition to the changes in the numerical solution, the economic aspects of the computation are analyzed and discussed below.

The CPU time requirements, which are obtained under batch mode operation of the VAX/1.2 computer system, are analyzed; an increase in the domain distances increases the necessary CPU time requirements.

3.2. Influence of number of nodes on the numerical solution

In the previous section, the effect of computational domain was studied by analyzing the computed velocities and pressures. It is clear that the numerical solutions are rather insensitive for domains beyond DD2. The CPU time requirement also favors the DD2 domain selection. Thus this section presents the influence of the number of grid nodes on the numerical solution, keeping the domain constant as DD2. Four additional sets of grid systems are generated as shown in Table 2, by increasing as well

as decreasing the grid set NN4 that was used in the previous section. Table 2 also provides the number of nodes for each direction. As the total number of nodes of the computation increases, the number of nodes in each direction also increases. The number of nodes along the longitudinal direction (x) increases more than the number along the other two directions.

A typical location at a distance $0.05L$ from the windward wall of the building was selected to analyze the local effect of nodes on the velocity and turbulence; the results are shown in Fig. 7. The vertical axis shows the node distance from the ground level normalized by the building height. Longitudinal velocity and square root of kinetic energy are normalized by the gradient velocity. Such non-dimensional values are shown in the horizontal axis. In both cases, the differences due to grids diminish with distance from the ground. Maximum turbulence values occur at $z/H = 1.0$, where the flow has high gradients due to its separation from the leading edge. The effect of the number of nodes on the velocities is clearly shown and this effect directly influences the computed turbulence values; these values are increased when the number of nodes are increased. On the other hand, for both variables only minimum changes are observed when the grids increase beyond 81,600 (NN4). Similar observations have been made for the other locations of the flow domain.

Pressure values in coefficient form have also been computed for different grid systems. Among the three walls, the influence of the nodes is pronounced for the side wall, where the flow is complex. As noted for the velocities and turbulence, the set NN4 is numerically optimum if one considers all the walls. When comparing the results from various grid sets with experimental data, even the NN3 grid set may be considered sufficient for the computations. However, further investigations and repetitive runs are necessary to generalize these observations.

Examination of the CPU time requirement in this case shows that the CPU time increases with an increase in the number of nodes. This may be due to additional operations needed by the process, to settle down. A similar increase in the CPU time was also observed for each

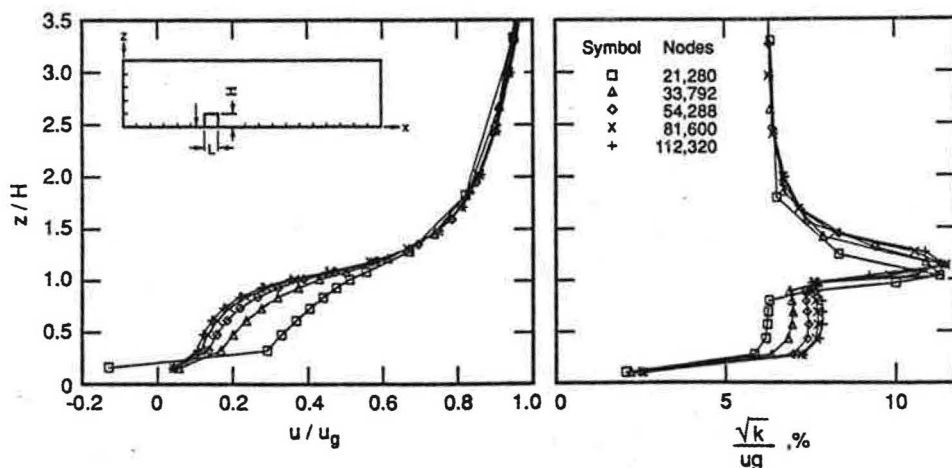


Fig. 7. Computed longitudinal velocity and turbulence intensity upstream of the building for different number of computational nodes.

iteration and this can easily be explained by considering the increased number of arithmetical operations. Moreover, the CPU time required is also influenced by the number of iterations performed, which itself increases with the number of nodes.

3.3. Effect of error level on the computed solution

For pressure-coupling schemes such as SIMPLE, the convergence of the numerical solution mainly depends on the under-relaxation factors and the acceptable error level of the solution. Patankar and Spalding [23], Gosman and Pun [35] and Patankar [24] performed sensitivity analysis for the under-relaxation factors. A set of optimum values were recommended for separated flows with recirculations and these factors were used in the present computation. Therefore, the influence of the under-relaxation factors on the computed result is not examined. Before presenting an acceptable error level for the numerical solution, it is useful to explain the interrelation of the term with the iterating procedure.

Conventionally, an iterating process is said to have converged when further iterations do not produce any change in the values of the dependent variables. Such a criterion may sometimes be misleading [3, 23]. When a heavy under-relaxation factor is used, the change in the dependent variable between successive iterations is slowed down. This may create a false convergence image, even though the current working solution is far from convergence. One way to overcome this numerical illusion is by monitoring how well the discretized equations are satisfied by the current value of the dependent variable and this can be conveniently performed as follows:

The residue of a particular iteration for node P can be obtained from equation (1) as:

$$R_\phi = \sum_{m=1}^{n_r} a_m \phi_m + S_L - a_P \phi_P \quad (2)$$

For a fully satisfied discretized equation, the L.H.S. of equation (2) has zero or near zero value. When ϕ_P takes the velocity variable (u , v and w) the calculated R_ϕ represents an imbalance in conservation of momentum. Since for the present study, the continuity equation is solved by using the SIMPLE algorithm, R_ϕ will represent an imbalance in the conservation of mass. Similarly, with the turbulence variable (k or ϵ), R_ϕ represents an imbalance in turbulence quantities.

In the present study, the convergence criterion was obtained based on the normalized error. Using equation (2), R_ϕ for each node is calculated and at the end of each iteration the summation of R_ϕ for all nodes is obtained. This is the total error of the iteration for the respective variable. The total error obtained for the first iteration is called the initial error of the computation. Then the normalized error is obtained by dividing the total error of each iteration by the initial error. For example, a normalized error of 0.7 reveals that the iteration process reached a stage where the initial error is reduced by 30%.

Such error levels are displayed in the vertical axis of Fig. 8, which has three curves representing the maximum value among the velocity variables (imbalance in the momentum), the error in pressure (imbalance in the con-

servation of mass) and the maximum value among the turbulence quantities. For the considered building geometry, the error is always higher in pressure than in the other variables. The same trend has been found for other buildings tested and this is probably due to the fact that a zero value is initially assumed for the unknown pressure field [24]. This is why most of the studies using the SIMPLE algorithm follow a convergence criterion based only on the imbalance of conservation of mass.

Another interesting feature observed in Fig. 8 is the reduction in error factor during the initial stage of the iteration process. A significant reduction of about 60% is found within the first 20 iterations; this steep gradient in reduction tends to slow down for further iterations. An increase of about 30 iterations (from 50 to 80) only reduces the normalized error to about 0.05. Therefore, termination of the process after 50 iterations was found to be reasonable. However, its consequences on the numerical solution as well as on the computational cost must be discussed.

Computations were performed based on four convergence criteria (0.4, 0.2, 0.1 and 0.05) without specifying any upper limit on the number of iterations. The DD2 computational domain and the NN4 grid set were used. The convergence criteria have a more pronounced effect on the computational cost as shown in Fig. 9. As expected, both the iterations and the CPU time increase when the normalized error levels are reduced. Based on the available limited data points, the curve can be divided into two segments at a point 0.1 on the x axis. The curve is steeper for the x axis region up to 0.1 in comparison to the region beyond 0.1. Thus the computational cost will increase significantly if one requires an error level less than 0.1.

Furthermore, the computed pressure and velocity values were analyzed as previously and found insensitive for the error factor beyond 0.1. Differences were noted between the results of 0.4 and 0.1 while only marginal changes were found in the computed results for 0.2 and 0.1 sets. Thus selecting 0.1 as the normalized error factor is reasonable, considering both the computed results and the cost. However, further research efforts are necessary to validate this observation by changing the other parameters, such as building height and inlet velocity profiles.

3.4. Influence of various computer systems

Computational runs have been carried out on three different micro-computers, namely AST Premium 386/20, DELL 286/20 and IPC 286/12, as well as on two mainframes VAX/1.2 and VAX/6.3. The specifications of the computer systems used in the present study are given in Table 3.

Keeping the size of the computational domain constant, the number of control volumes inside the domain has been varied to establish the parameters for economical computation. Simulations were made on each computer system based on its capacity limits. Figure 10 presents the results; the CPU time needed only for module 2 is plotted as a function of the number of grid nodes (see Fig. 3). The CPU time for the microcomputers represents the direct, continuous access time whereas the CPU time for VAX machines is taken under batch mode

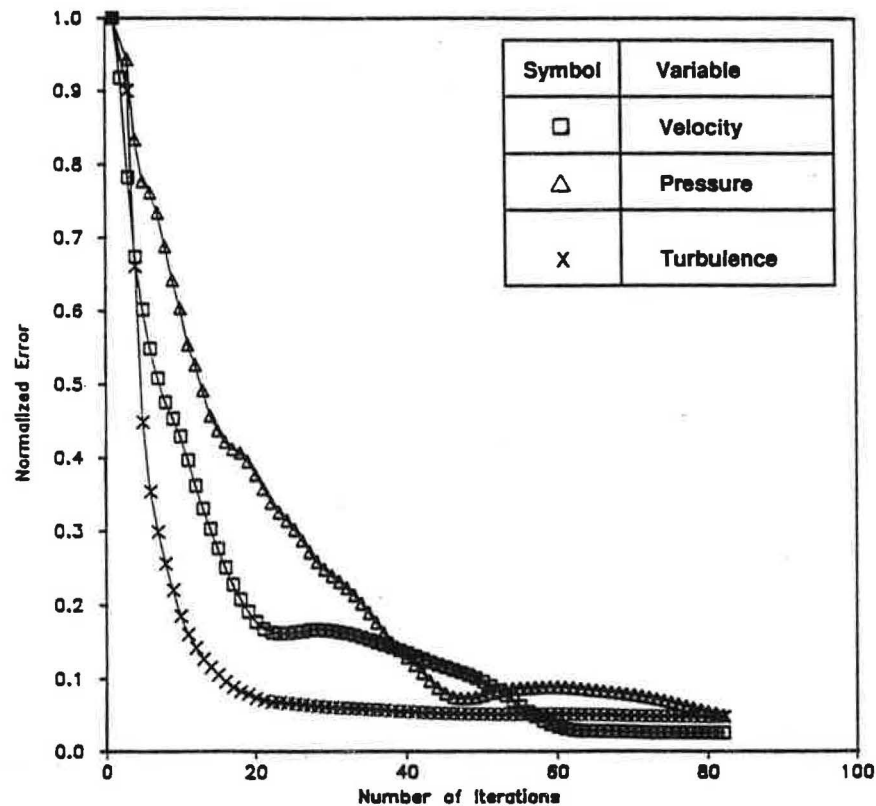


Fig. 8. Reduction in the normalized error level for different variables of computation.

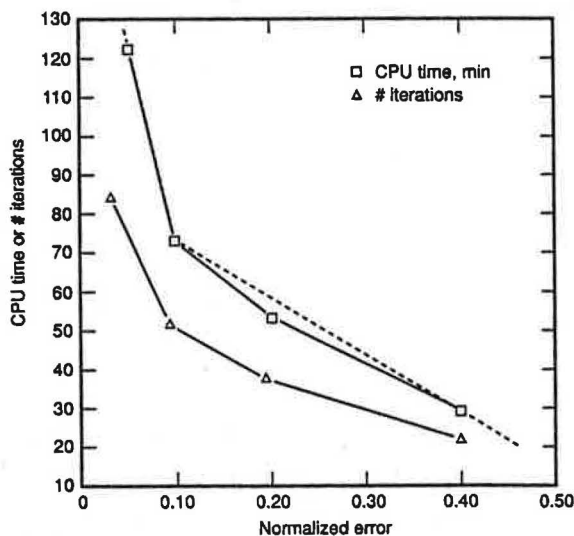


Fig. 9. Effect of normalized error on the CPU time and on the number of iterations.

operation. Microcomputers with longer word length and higher clock speed consume less CPU time, as expected. On the other hand, the hard disk access time does not affect the CPU time, due to the iterating nature of the problem. Both IPC 286/12 and DELL 286/20 have the same Intel 286 microprocessor but the high clock speed

DELL takes less CPU time. It is also interesting to note that both DELL and AST have the same speed but the AST, with longer word length, consumes less CPU time.

The VAX machines operate with the unique page faulting and virtual memory address technology. However, the difference in MIPS (millions of instructions per second) does not directly affect the CPU time. In fact,

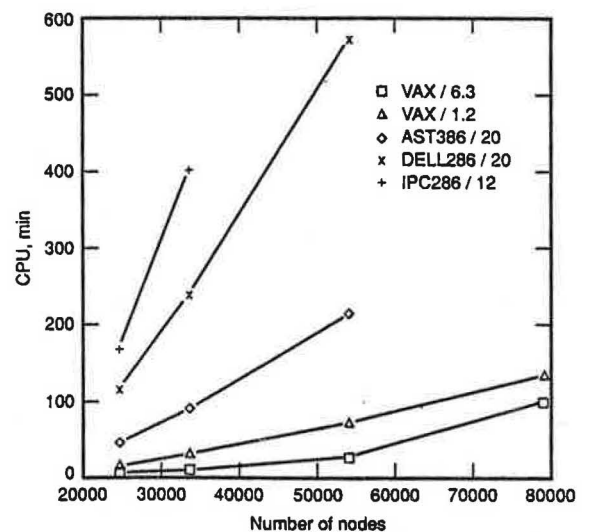


Fig. 10. CPU time taken by TWIST for test runs with different computational grids.

Table 3. Specifications of the computer systems used in the present study

Model	Word length (Bits)	Clock speed (mHz)	Hard disk access time (ms)	Accessories
IPC AT 286 (1986)	16	12	24	MS-Dos Operating System V3.3 MS-Fortran Compiler V4.0 Linker V5.1 287 Math Co-processor
DELL AT 286 (1988)	16	20	29	"
AST Premium 386 (1988)	32	20	15	MS-Dos Operating System V3.3 MS-Fortran Compiler V4.0 Linker V5.1 387 Math Co-processor
VAX 11/785	32	1.2 MIPS	N/A	VMS-Operating System V5.01 VMS-Fortran Compiler V4.8 Linker V5.1
VAX 8550	32	6.3 MIPS	N/A	"

the following relationships have been formulated for the CPU time required to run the test case :

$$\begin{aligned}
 t[\text{VAX}/1.2] &\approx 3 * t[\text{VAX}/6.3] \\
 t[386/20] &\approx 9 * t[\text{VAX}/6.3] \\
 t[286/20] &\approx 24 * t[\text{VAX}/6.3] \\
 t[286/12] &\approx 36 * t[\text{VAX}/6.3]. \quad (3)
 \end{aligned}$$

A simulation takes about 20 minutes (CPU time) to run in the VAX/6.3 with 54,288 grid nodes. From the discussion two features become evident; one is that microcomputers require a CPU time 9 to 36 times higher than the time necessary for the same run in the VAX machines. Secondly, the CPU time required for computation increases quasi-linearly with the number of grid nodes.

As discussed in the previous section, another significant computing parameter is the error level of convergence. Figure 11 displays the largest normalized error level value among the six variables (u, v, w, p, k, ϵ) for the respective number of iterations with 54,288 nodes in the computational domain. Clearly, the CPU time required for different computers increases when the error levels are reduced. Furthermore, the smaller the computer system the more drastic this increase appears to be. It can be concluded that the error levels have direct influence on the number of iterations required and hence on the CPU time.

Computed pressures and velocities have also been analyzed and no significant difference has been noticed among the results of the various systems. In fact, the 32

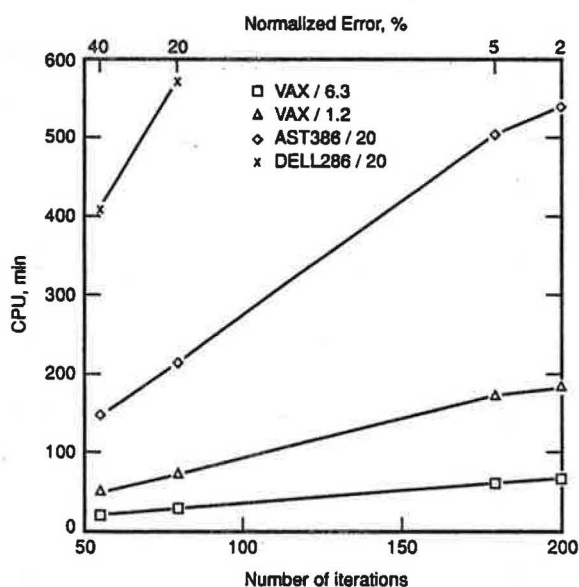


Fig. 11. CPU time taken by TWIST for test runs with different number of iterations.

bit machine with Intel 387 math co-processor computes exactly the same numerical results as the VAX machines.

4. CONCLUSIONS

A systematic analysis has been performed to identify the influence of the computing parameters in the numerical modelling of wind flow conditions around buildings. This will be useful in developing a diagnostic system

for the computed results. Based on this analysis, the following conclusions can be made:

- (1) The number of computational nodes affects the computed results as well as the computational time
- (2) The error of the unknown pressure field dominates the convergence of the iterating process.
- (3) Economical computations can be achieved by using 32 bit machines with high clock speeds.

REFERENCES

1. D. Vasilic-Melling, Three Dimensional Turbulent Flow Past Rectangular Bluff Bodies, Ph.D. Thesis, Imperial College of Science and Technology, London (1977).
2. T. Hanson, D. M. Summers and C. B. Wilson, Numerical modelling of wind flow over buildings in two dimensions, *Int. J. Num. Meth. Fluids* 4, 25-41 (1984).
3. T. Hanson, D. M. Summers and C. B. Wilson, A three-dimensional simulation of wind flow around buildings, *Int. J. Num. Meth. Fluids* 6, 113-127 (1986).
4. D. M. Summers, T. Hanson and C. B. Wilson, Validation of a computer simulation of wind flow over a building model, *Bldg Envir.* 21, 97-111 (1986).
5. D. A. Paterson and C. J. Apelt, Computation of wind flows over three-dimensional buildings, *J. Wind Engng Ind. Aerodyn.* 24, 193-213 (1986).
6. D. A. Paterson and C. J. Apelt, Simulation of wind flow around three-dimensional buildings, *Bldg Envir.* 24, 39-50 (1989).
7. S. Murakami, A. Mochida and K. Hibi, Three dimensional numerical simulation of air flow around a cubic model by means of large eddy simulation, *J. Wind Engng Ind. Aerodyn.* 25, 291-305 (1987).
8. S. Murakami and A. Mochida, Three-dimensional numerical simulation of turbulent flow around buildings using $k-\epsilon$ turbulence model. *Bldg Envir.* 24, 51-64 (1989).
9. E. H. Mathews and J. P. Meyer, Numerical modelling of wind loading on a film clad greenhouse, *Bldg Envir.* 22, 129-134 (1987).
10. F. Baetke, Numerische Berechnung der Turbulenten Umströmung eines kubischen Körpers, Ph.D. Thesis, Technische Universität München, Germany (1986).
11. A. Baskaran and T. Stathopoulos, Computational evaluation of wind effects on buildings, *Bldg Envir.* 24, 325-333 (1989).
12. A. Baskaran, Computer Simulation of 3D Turbulent Wind Effects on Buildings, Ph.D. Thesis, Concordia University, Montreal, Canada (1990).
13. J. C. R. Hunt, Studying turbulence using direct numerical simulation: 1987 Center for Turbulence, NASA Ames/Stanford Summer Programme, *J. Fluid Mech.* 190, 375-392 (1988).
14. A. D. Gosman and K. Y. M. Lai, Finite-Difference and Other Approximations for the Transport and Navier-Stokes Equations, Proceedings of IAHR Symposium on Refined Modelling of Flows, Paris (1982).
15. G. D. Raithby, A critical evaluation of upstream differencing applied to problems involving fluid flow, *Comp. Meth. Appl. Mech. Engng* 9, 75-103 (1976).
16. M. A. Leschziner, Practical evaluation of three finite difference schemes for the computation of steady-state recirculating flows, *Comp. Methods Appl. Mech. Engng* 23, 293-312 (1980).
17. B. E. Launder and D. B. Spalding, *Lectures in Mathematical Model of Turbulence*, Academic Press, London (1972).
18. W. Rodi, The Prediction of Free Turbulent Boundary Layers by Use of a Two-Equation Model of Turbulence, Ph.D. Thesis, Imperial College of Science and Technology, London (1972).
19. D. B. Spalding, Turbulence Models, A Lecture Course, Report No. CFD/82/4, Computational Fluid Dynamics Unit, Imperial College of Science and Technology, London (1982).
20. T. W. Everett and T. V. Lawson, Wind-Tunnel Measurements of Pressure and Velocity around a Simple Building in a Turbulent Shear Flow to Allow Validation of Values derived from a Computer Solution of the Navier-Stokes Equations, Department of Aeronautical Engineering, Rep. No. TVL/8401, Bristol University (1984).
21. P. J. Richards, Computational Modelling of Wind Flow around Low-Rise Buildings Using PHOENICS, Report No. DN1508, AFRC Institute of Engineering Research, Wrest-Park, Silsoe, Bedford, U.K. (1989).
22. D. B. Spalding, A general purpose computer program for multi-dimensional one and two-phase flow, *Math. and Comp. Simulation XXIII*, 267-276 (1981).
23. S. V. Patankar and D. B. Spalding, A calculation procedure for heat, mass and momentum transfer in three-dimensional parabolic flows, *Int. J. Heat Mass Transfer* 15, 1787-1806 (1972).
24. S. V. Patankar, *Numerical Heat Transfer and Fluid Flow*, McGraw-Hill, London (1980).
25. B. E. Launder and D. B. Spalding, The numerical computation of turbulent flows, *Comp. Methods App. Mech. Engng* 3, 269-289 (1974).
26. T. Stathopoulos and A. Baskaran, Boundary treatment for the computation of 3D turbulent conditions around buildings, *J. Wind Engng Ind. Aerodyn.* 35, 177-200 (1990).
27. J. C. R. Hunt and G. P. Smith, A Theory of Wakes behind Buildings and some Provisional Experimental Results, C.E.G.B. Lab. Note, RD/L/N3169, Central Electricity Research Laboratories, Leatherhead, England (1969).
28. J. C. R. Hunt, Further Aspects of the Theory of Wakes behind Buildings and a Comparison of the Theory with Experimental Results, C.E.G.B. Lab. Note, RD/L/R1665, Central Electricity Research Laboratories, Leatherhead, England (1970).
29. R. Lemberg, On the Wakes behind Bluff Bodies in a Turbulent Boundary Layer, Ph.D. Thesis, University of Western Ontario, Canada (1973).
30. A. P. Penwarden and A. F. W. Wise, Wind Environment Around Buildings, BRE Report, HMSO, U.K. (1973).
31. J. Gandemer, Wind Environment around Buildings: Aerodynamic Concepts, *Proceedings of the 4th Int. Conf. on Wind Engng*, Heathrow, London (1975), 423-432.

32. W. J. Beranek, General Rules for the Determination of Wind Environment, *Proceedings of the 5th Int. Conf. on Wind Engng*, Fort Collins, Colorado, U.S.A., 1 (1979), 225-235.
33. J. Antoniou and G. Bergeles, Development of the reattached flow behind surface-mounted two-dimensional prisms, *Transactions of ASME, J. Fluids Engng* **110**, 127-133 (1984).
34. G. Bergeles and N. Athanassiadis, The flow past a surface-mounted obstacle, *Transactions of ASME, J. Fluids Engng* **105**, 461-463 (1983).
35. A. D. Gosman and W. M. Pun, KASE Problems for the TEACH Computer Programs, Report No, HTS/74/3, Department of Mech. Engng, Imperial College of Science and Technology, London (1974).