

# Towards Real-Time Model-Based Monitoring and Adoptive Controlling of Indoor Thermal Comfort

Ali Youssef<sup>\*1</sup>, Pieter Truyen<sup>1</sup>, Peter Bröde<sup>2</sup>, Dusan Fiala<sup>3</sup>, and Jean-Marie Aerts<sup>1</sup>

<sup>1</sup> *KU Leuven, M3-BIORES  
Kasteelpark Arenberg 30 bus 2456  
3001 Heverlee, Belgium*

<sup>2</sup> *Leibniz Research Centre for Working Environment  
and Human (ifADo)  
Ardeystraße 67  
44139 Dortmund, Germany*

<sup>3</sup> *Institute for Building Materials, Building Physics,  
Building Technology and Design (IBBTE)  
Keplerstraße 11  
D-70174 Stuttgart, Germany*

## ABSTRACT

Thermal comfort is an important aspect of the building design and indoor climate control as modern man spends most of the day indoors. Conventional indoor climate design and control approaches are based on static thermal comfort models that views the building occupants as passive recipients of their thermal environment. Assuming that people have relatively constant range of biological comfort requirements, and that the indoor environmental variables should be controlled to conform to that constant range. The (r)evolution in modern sensing and computing technologies (price, compact size, flexibility and stretchability) is making it possible to continuously measure signals in real-time from human body using wearable technologies and smart clothing. Many advanced and accurate mechanistic thermoregulation models, such as the 'Fiala thermal Physiology and Comfort' model, are developed to assess the thermal strains and comfort status of humans. However, the most reliable mechanistic models are too complex to be implemented in real-time for monitoring and control applications. Additionally, such models are using not-easily or invasively measured variables (e.g., core temperatures), which are often not practical and undesirable measurements for monitoring during varied activities over prolonged periods. The purpose of this work is to develop a databased mechanistic (grey box) model, with minimum number of parameters and non-invasive input variables, for real-time monitoring and controlling of individual occupant's thermal comfort. Eight healthy males (mean  $\pm$  standard deviation: age  $22.8 \pm 1.3$  years, height  $1.81 \pm 0.06$ m, body surface area  $1.94 \pm 0.11$  m<sup>2</sup>) are used as test subjects to perform the designed experiments. The experimental protocol involved step-changes of exercise on treadmill inside to simulate step-changes in activity level. Metabolic heat production was calculated based on the continuously measured O<sub>2</sub> consumption and CO<sub>2</sub> production. Rectal temperature are continuously measured. Mean clothing layer and mean skin temperatures were calculated based on measured temperatures from eight body locations. The experiments were performed with the subjects wearing dry and wet underwear layer and constant ventilation rate. First-order multi-inputs-single-output discrete time transfer function, with only mean skin temperature and metabolic heat production or mean underwear temperature as inputs, was found to be the best to describe the dynamic responses of the rectal temperature. That with average coefficient of determination  $R^2 = 0.96 \pm 0.2$  and average Young Identification Criterion  $YIC = -9.20 \pm 4.2$ . to The resulted models were compact enough (two inputs) to be implemented in real-time. Hence, the resulted model

structure can be implemented in closed-loop algorithm for online identification of the model and parameters estimation is foreseen to be employed for occupant-based climate control applications and smart clothing.

## KEYWORDS

thermal comfort, indoor climate control, dynamic modelling, model-based control

## 1 INTRODUCTION

Thermal comfort is an important aspect of the building design and indoor climate control as modern man spends most of the day indoors. Conventional indoor climate design and control approaches are based on static thermal comfort models that views the building occupants as passive recipients of their thermal environment. the primary purpose of HVAC was to maintain constant thermal environmental conditions throughout the interior aiming for an optimum 'steady-state' temperature setting based on Fanger's Predicted Mean Vote and Predicted Percentage Dissatisfied (PMV-PPD) model (Fanger, 1970; Parsons, 2014). Many advanced and accurate mechanistic thermoregulation models, such as the 'Fiala thermal Physiology and Comfort' model, are developed to assess the thermal strains and comfort status of humans (Havenith and Fiala, 2015). Most accurate and reliable models however, are too complex to enable real-time monitoring and control of the environmental conditions. Therefore, new models need to be found that are both simple and accurate. Early detection of core body temperature gain is key to the implementation of suitable strategies (i.e. cooling) to avoid exertional heat stroke (Niedermann et al., 2014). However, on the one hand, existing methods are invasive (inserting rectal or oesophageal temperature probes, etc.) and not convenient for long-term monitoring due to subject discomfort. On the other hand, the application of noninvasive measurement methods (tympanic membrane, oral, axillary) have demonstrated only limited accuracy for use in working environments. Most of the current methods to measure and predict the core body temperature in comparison to the rectal temperature method, neither meet the requirement of an accurate measurement of the core body temperature ( $\pm 0.1$  °C) nor do they enable the continuous measurement of the core body temperature in changing working conditions (Niedermann et al., 2014). Therefore, the purpose of this work was to develop a an adaptive dynamic model with minimum number of parameters and non-invasive input variables, to predict the core body temperature for real-time monitoring and controlling of individual occupant's thermal comfort.

## 2 MATERIALS AND METHODS

### 2.1 Experiments and test subjects

The data used in this paper was obtained from conducted human experiments at Leibniz Research Centre for Working Environment and Human Factors at the University of Dortmund (*IfADo*) (Bröde et al., 2008; Niedermann et al., 2014). During these experiments, measurements from eight healthy male students (mean  $\pm$  standard deviation: age  $22.8 \pm 1.3$  years, body height  $1.81 \pm 0.06$  m, body mass  $75.1 \pm 6.6$  kg and body surface area  $1.94 \pm 0.11$  m<sup>2</sup>) were collected. In order to reduce the evaporation to the environment, the experiments were carried out under a high humidity condition with air temperature ( $T_a$ ) of 20 °C, relative humidity ( $RH$ ) of 80%, yielding ambient water vapour pressure ( $P_a$ ) of 1.87 kPa, and air velocity of 0.5 ms<sup>-1</sup>. Globe temperature was equal to  $T_a$ . The subjects wore their own briefs, socks and sport shoes, and a four layer clothing ensemble consisting of polypropylene underwear (HHS, Helly Hansen Super Bodywear 140 g.m<sup>-2</sup>), a hooded TYCHEM ® C Standard coverall as intermediate layer

preventing both wicking and evaporation, additional cotton (CO, type ‘‘Gnägi’’, Switzerland) mid layer and an impermeable PVC outer layer. Trials were performed with the CO mid layer either dry (dry condition) or wetted using  $618 \pm 16$  g of water (wet condition). The sequence of those conditions was balanced across subjects who visited the laboratory at the same time of day (for more information about the experiments see Bröde et al. 2008; Niedermann et al. 2014). The experimental protocol itself contained of a 30-minute resting phase followed by three phases inside a climatic chamber, each lasting 30 minutes and separated by a 3-minute period where the fully clothed person’s weight was determined. The first exercising phase comprised of 2 minutes of treadmill walking at  $4.5 \text{ km}\cdot\text{h}^{-1}$  followed by 28 minutes of standing in the room. Treadmill work was performed during the second and third phase.

## 2.2 Measurements

Metabolic heat production rate ( $Q_{met}$ ,  $\text{W}\cdot\text{m}^{-2}$ ) was calculated according to ISO 8996 (ISO, 2004) from the analysis of  $\text{O}_2$  consumption (Servomex Series 1100, Servomex Ltd., UK) and  $\text{CO}_2$  production (UNOR Infrarot-Gasanalysator, maihak AG, Germany) of expired air collected with Douglas bags during the last 10 minutes of phases 1 and 3, respectively. Mean skin temperature ( $T_{skm}$ ,  $^{\circ}\text{C}$ ) was calculated as the average of thermistor recordings (YSI 427, Yellow Springs, USA) at eight body sites (forehead, left chest, right frontal thigh, left dorsal thigh, right scapula, right upper arm, left lower arm and left hand) according to a variant of the ISO 9886 scheme (ISO, 1992). The rectal temperatures ( $T_{re}$ ,  $^{\circ}\text{C}$ ) were continuously recorded with a flexible thermistor probe at a depth of 10 cm from the anal sphincter (YSI 401, Yellow Springs, USA). Water vapour pressure ( $uwP_{air}$ , kPa) and air temperature ( $uwT_{air}$ ,  $^{\circ}\text{C}$ ) in the clothing’s microclimate were measured by data loggers (HandyLog DK502, Driesen + Kern GmbH, Germany) positioned at the right chest and left scapula between the underwear HHS layer and TYCHEM® layer and, correspondingly, at the contra lateral sites between the CO mid and PVC outer layer. An example of the different measured variables during the conducted experiments is shown in Figure 1 for subject #1 under dry conditions.

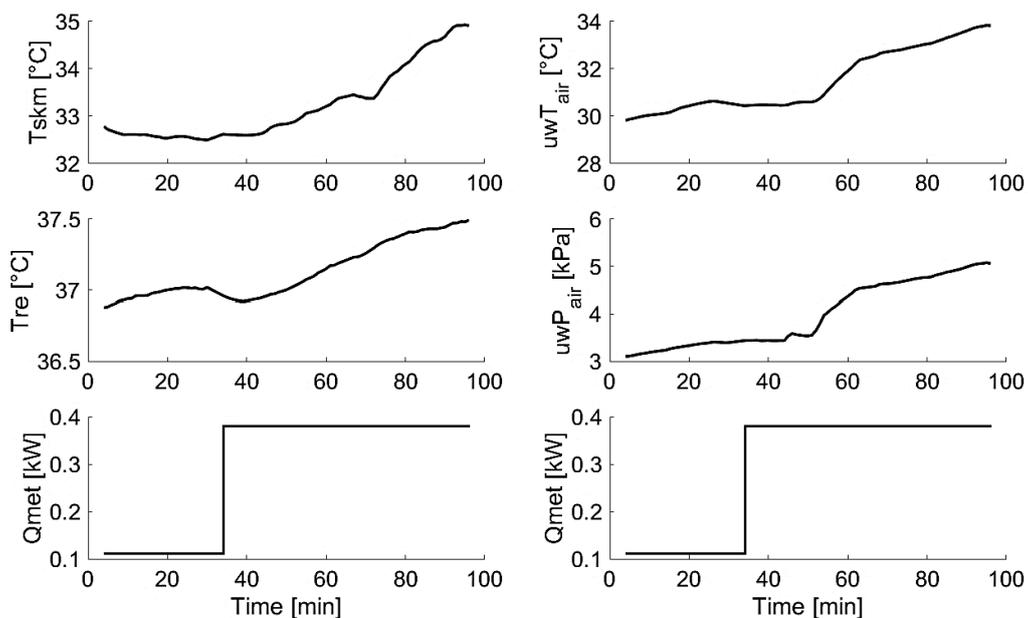


Figure 1. The dynamic response of mean skin temperature ( $T_{skm}$ ,  $^{\circ}\text{C}$ ), rectal temperature ( $T_{re}$ ,  $^{\circ}\text{C}$ ), mean underwear air temperature ( $uwT_{air}$ ,  $^{\circ}\text{C}$ ) and mean underwear water vapour pressure ( $uwP_{air}$ , kPa) to step increase in the metabolic heat production rate ( $Q_{met}$ , kW) for test subject #1 at dry conditions.

## 2.3 System identification and online modelling

The human system is considered as Complex, Individually different, Time varying and Dynamic (CITD) systems (Quanten et al., 2006; Youssef et al., 2014). Although the system (body thermoregulation) under study is inherently a non-linear system, the essential perturbation behaviour can often be approximated well by simple linearized transfer function (TF) models (Young et al., 1991; Youssef, 2014). The dynamic responses of the core body temperature, represented by the measured rectal temperature  $T_{re}$ , is modelled using different input variables using both single-input-single-output (SISO) and multiple-input-single-output (MISO) discrete-time transfer function (DTF). Mean skin temperature  $T_{skm}$ , mean underwear temperature  $uwT_{air}$ , underwear water vapour pressure  $uwP_{air}$  and metabolic heat production  $Q_{met}$  are considered separately and combined as input variables to model the rectal temperature  $T_{re}$ . For the purposes of the present paper, therefore, the following linear, discrete-time-system was considered,

$$T_{re}(k) = \sum_{i=1}^{nu} \frac{B_i(z^{-1})}{A(z^{-1})} u_i(k - \delta_i) + \xi(k) \quad (1)$$

where,

$$\begin{aligned} A(z^{-1}) &= 1 + a_1 z^{-1} + a_2 z^{-2} + \dots + a_n z^{-n} \\ B_i(z^{-1}) &= b_{0,i} + b_{1,i} z^{-1} + b_{2,i} z^{-2} + \dots + b_{m,i} z^{-m} \end{aligned} \quad (2)$$

where  $T_{re}(k)$  is the model output and  $u_i(k)$  is the  $i^{\text{th}}$  model input, while  $A(z^{-1})$  and  $B_i(z^{-1})$  are appropriately defined polynomials in the backshift operator  $z^{-1}$ , i.e.,  $z^{-i}y(k) = y(k - i)$ . While,  $nu$  is number of model inputs (i.e.,  $nu = 1$  for SISO and  $nu > 1$  for MISO systems) and  $\xi(k)$  is additive noise, a serially uncorrelated sequence of random variables with variance  $\sigma^2$  that accounts for measurement noise, modelling errors and effects of unmeasured inputs to the process (assumed to be a zero mean). The simplified refined instrumental variable (SRIV) algorithm was utilised in the identification and estimation of the models (model parameters and model structure) (Young et al., 2000; Young and Jakeman, 1980). The appropriate model structure was identified, i.e., the most appropriate values for the triad  $[n, m, \delta]$  (see equations 1 and 2). Two main statistical measures were employed to determine the most appropriate values of this triad. Namely, the coefficient of determination  $R_2^T$ , based on the response error; and  $YIC$  (Young's Information Criterion), which provides a combined measure of model fit and parametric efficiency, with large negative values indicating a model which explains the output data well and yet avoids over-parameterisation (Young, 2011). The modelling procedures were applied on the data from both dry and wet conditions.

## 3 RESULTS AND DISCUSSIONS

### 3.1 Model identification

#### - Dry condition

The SRIV algorithm combined with the root mean square error (RMSE),  $YIC$  and  $R_2^T$  suggested, in general, that a first order (number of poles,  $n = 1$ ) MISO DTF models, including the metabolic heat production  $Q_{met}$  and mean skin temperature  $T_{skm}$  as model inputs (i.e.,  $nu = 2$ ), described the dynamic responses of the rectal temperature  $T_{re}$  most accurately (i.e.,  $R_2^T = 0.98 \pm 0.17$  and  $YIC = -7.63 \pm 2.40$ ). More specifically, the SRIV algorithm identified the following general discrete-time TF model structure represented by the triad  $[1 \ 1 \ 1 \ \delta_1 \ \delta_2]$ ,

$$T_{re}(k) = \left[ \frac{B_1(z^{-1})}{A(z^{-1})} \frac{B_2(z^{-1})}{A(z^{-1})} \right] \cdot \begin{bmatrix} Q_{met}(k-\delta_1) \\ T_{skm}(k-\delta_2) \end{bmatrix} + \xi(k) \quad (3)$$

where the time delays  $\delta_1$  and  $\delta_2$  were different from test subject to another (Table 1).

Table 1. The resulted MISO model structures  $[n \ m_1 \ m_2 \ \delta_1 \ \delta_2]$  and the mean estimated polynomials  $A(z^{-1})$ ,  $B_1(z^{-1})$  and  $B_2(z^{-1})$  with metabolic heat production  $Q_{met}$  and mean skin temperature  $T_{skm}$  as model inputs, showing the mean model identification criteria  $R_2^T$ , YIC and RMSE for all the test subjects under dry condition.

	$n$	$m_1$	$m_2$	$\delta_1$	$\delta_2$	$A(z^{-1})$	$B_1(z^{-1})$	$B_2(z^{-1})$	$R_2^T$	YIC	RMSE
<b>Mean</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>5</b>	<b>4</b>	<b>0.05</b>	<b>0.0012</b>	<b>0.0026</b>	<b>0.98</b>	<b>-7.63</b>	<b>0.007</b>
$\pm$ Standard deviation	<b>1</b>	<b>1</b>	<b>1</b>	$\pm 4$	$\pm 3$	$\pm 0.076$	$\pm 3.50 \times 10^{-4}$	$\pm 0.010$	$\pm 0.17$	$\pm 2.40$	$\pm 2.70 \times 10^{-4}$

Additionally, the results have shown that a first MISO DTF models, with the mean skin temperature  $T_{skm}$  and the mean underwear temperature  $uwT_{air}$  as model inputs, were able to describe the dynamic responses of the rectal temperature  $T_{re}$  sufficiently (i.e.,  $R_2^T = 0.95 \pm 0.05$  and  $YIC = -9.66 \pm 3.22$ ). More specifically, the SRIV algorithm identified the following general discrete-time TF model structure represented by the triad  $[1 \ 1 \ 1 \ \delta_1 \ \delta_2]$ ,

$$T_{re}(k) = \left[ \frac{B_1(z^{-1})}{A(z^{-1})} \frac{B_2(z^{-1})}{A(z^{-1})} \right] \cdot \begin{bmatrix} T_{skm}(k-\delta_1) \\ uwT_{air}(k-\delta_2) \end{bmatrix} + \xi(k) \quad (4)$$

The mean estimated model polynomials,  $A(z^{-1})$ ,  $B_1(z^{-1})$  and  $B_2(z^{-1})$ , resulted from the data from all the eight test subjects are presented in Table 2.

Table 2. The resulted MISO model structures  $[n \ m_1 \ m_2 \ \delta_1 \ \delta_2]$  and the mean estimated polynomials  $A(z^{-1})$ ,  $B_1(z^{-1})$  and  $B_2(z^{-1})$  with mean skin temperature  $T_{skm}$  and mean underwear temperature  $uwT_{air}$  as model inputs, showing the mean model identification criteria  $R_2^T$ , YIC and RMSE for all the test subjects under dry condition.

	$n$	$m_1$	$m_2$	$\delta_1$	$\delta_2$	$A(z^{-1})$	$B_1(z^{-1})$	$B_2(z^{-1})$	$R_2^T$	YIC	RMSE
<b>Mean</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	<b>4</b>	<b>0.25</b>	<b>0.052</b>	<b>0.0030</b>	<b>0.95</b>	<b>-5.63</b>	<b>0.022</b>
$\pm$ Standard deviation	<b>1</b>	<b>1</b>	<b>1</b>	$\pm 2$	$\pm 3$	$\pm 0.22$	$\pm 4.2 \times 10^{-3}$	$\pm 0.023$	$\pm 0.05$	$\pm 3.25$	$\pm 1.85 \times 10^{-3}$

#### - **Wet condition**

The same MISO model structure, as resulted for the dry condition (i.e.,  $[1 \ 1 \ 1 \ \delta_1 \ \delta_2]$ ), was best to describe the dynamic responses of the rectal temperature of all the test subjects under wet condition (see Tables 3 and 4).

Table 3. The resulted MISO model structures  $[n \ m_1 \ m_2 \ \delta_1 \ \delta_2]$  and the mean estimated polynomials  $A(z^{-1})$ ,  $B_1(z^{-1})$  and  $B_2(z^{-1})$  with metabolic heat production  $Q_{met}$  and mean skin temperature  $T_{skm}$  as model inputs, showing the mean model identification criteria  $R_2^T$ , YIC and RMSE for all the test subjects under wet condition.

	$n$	$m_1$	$m_2$	$\delta_1$	$\delta_2$	$A(z^{-1})$	$B_1(z^{-1})$	$B_2(z^{-1})$	$R_2^T$	YIC	RMSE
<b>Mean</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>4</b>	<b>7</b>	<b>0.03</b>	<b>0.00017</b>	<b>-0.015</b>	<b>0.98</b>	<b>-8.88</b>	<b>0.03</b>
$\pm$ Standard deviation	<b>1</b>	<b>1</b>	<b>1</b>	$\pm 3$	$\pm 3$	$\pm 0.010$	$\pm 5.42 \times 10^{-5}$	$\pm 0.007$	$\pm 0.15$	$\pm 1.63$	$\pm 4.42 \times 10^{-3}$

Table 4. The resulted MISO model structures [ $n$   $m_1$   $m_2$   $\delta_1$   $\delta_2$ ] and the mean estimated polynomials  $A(z^{-1})$ ,  $B_1(z^{-1})$  and  $B_2(z^{-1})$  with mean skin temperature  $T_{skm}$  and mean underwear temperature  $uwT_{air}$  as model inputs, showing the mean model identification criteria  $R_2^T$ , YIC and RMSE for all the test subjects under wet condition.

	$n$	$m$	$m$	$\delta_1$	$\delta_2$	$A(z^{-1})$	$B_1(z^{-1})$	$B_2(z^{-1})$	$R^2$	YIC	RMSE
<b>Mean</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>4</b>	<b>6</b>	<b>0.21</b>	<b>0.052</b>	<b>0.0030</b>	<b>0.95</b>	<b>-5.63</b>	<b>0.022</b>
$\pm$ Standard deviation	<b>1</b>	<b>1</b>	<b>1</b>	$\pm 2$	$\pm 3$	$\pm 0.32$	$\pm 4.2 \times 10^{-3}$	$\pm 0.023$	$\pm 0.05$	$\pm 3.25$	$\pm 1.85 \times 10^{-3}$

The results showed that a higher time delays ( $\delta_1$   $\delta_2$ ) in case of wet condition in comparison to dry conditions. The used SRIV algorithm is suitable to be run in closed-loop for online model estimation. One of the main advantages of the above mentioned approach is that it is automatically accommodating with the multiple-time delays that were observed with the various identified TF models for different test subjects.

## 4 CONCLUSIONS

Eight healthy males (mean  $\pm$  standard deviation: age  $22.8 \pm 1.3$  years, height  $1.81 \pm 0.06$ m, body surface area  $1.94 \pm 0.11$  m<sup>2</sup>) are used as test subjects to perform the designed experiments. The experimental protocol involved step-changes of exercise on treadmill inside to simulate step-changes in activity level. Metabolic heat production was calculated based on the continuously measured O<sub>2</sub> consumption and CO<sub>2</sub> production. Rectal temperature are continuously measured. Mean clothing layer and mean skin temperatures were calculated based on measured temperatures from eight body locations. The experiments were performed with the subjects wearing dry and wet underwear layer and constant ventilation rate. First order MISO DTF models were found to be the most suitable (i.e.,  $R_2^T = 0.96 \pm 0.2$  and  $YIC = -9.20 \pm 4.2$ ) to describe the dynamic response of the rectal temperature of the tested subjects under both dry and wet conditions. Paring the mean skin temperature  $T_{skm}$ , with the mean underwear temperature  $uwT_{air}$  once and with the metabolic heat production  $Q_{met}$  another, was found the most suitable model inputs to the MISO DTF. It is suggested to use the mean skin temperature  $T_{skm}$  with the mean underwear temperature  $uwT_{air}$  for online prediction of the rectal temperature and further model-based controlling of the body thermal comfort.

## 5 REFERENCES

- Bröde, P., Havenith, G., Wang, X., Candas, V., den Hartog, E.A., Griefahn, B., Holmér, I., et al. (2008), "Non-evaporative effects of a wet mid layer on heat transfer through protective clothing", *European Journal of Applied Physiology*, Vol. 104 No. 2, pp. 341–349.
- Fanger, P.O. (1970), *Thermal Comfort : Analysis and Applications in Environmental Engineering*, 1st ed., Danish Technical Press, Lyngby.
- Havenith, G. and Fiala, D. (2015), "Thermal Indices and Thermophysiological Modeling for Heat Stress", *Comprehensive Physiology*, Vol. 6, John Wiley & Sons, Inc., Hoboken, NJ, USA, pp. 255–302.
- Niedermann, R., Wyss, E., Annaheim, S., Psikuta, A., Davey, S. and Rossi, R.M. (2014), "Prediction of human core body temperature using non-invasive measurement methods", *International Journal of Biometeorology*, Springer Berlin Heidelberg, Vol. 58 No. 1, pp. 7–15.

- Parsons, K.C. (Kenneth C.. (2014), *Human Thermal Environments : The Effects of Hot, Moderate, and Cold Environments on Human Health, Comfort, and Performance*, 3rd ed., CRC Press.
- Quanten, S., de Valck, E., Cluydts, R., Aerts, J.-M. and Berckmans, D. (2006), “Individualized and time-variant model for the functional link between thermoregulation and sleep onset.”, *Journal of Sleep Research*, Vol. 15 No. 2, pp. 183–98.
- Young, P., Price, L., Berckmans, D. and Janssens, K. (2000), “Recent developments in the modelling of imperfectly mixed airspaces”, *Computers and Electronics in Agriculture*, ELSEVIER SCIENCE BV, Vol. 26 No. 3, pp. 239–254.
- Young, P.C. (2011), *Recursive Estimation and Time-Series Analysis: An Introduction for the Student and Practitioner*, Springer.
- Young, P.C., Chotai, A. and Tych, W. (1991), “Identification, estimation and control of continuous-time systems described by delta operator models.”, Kluwer Academic Publishers, 28 April.
- Young, P.C. and Jakeman, A. (1980), “Refined instrumental variable methods of recursive time-series analysis Part III. Extensions”, *International Journal of Control*, Taylor & Francis, Vol. 31 No. 4, pp. 741–764.
- Youssef, A. (2014), *Model-Based Control of Micro-Environment with Real-Time Feedback of Bioresponses*, KU Leuven.
- Youssef, A., Exadaktylos, V. and Berckmans, D. (2014), “Modelling and quantification of the thermoregulatory responses of the developing avian embryo: Electrical analogies of a physiological system”, *Journal of Thermal Biology*, Vol. 44, pp. 14–19.